



## I. AUTOCORRELATIONS

The autocorrelation function is defined as

$$E[x(t_1)x(t_0)] - E[x(t_1)]E[x(t_0)]$$

where  $t_0, t_1$  are times of propagation of the Markov chain. And  $E$  is an average over an ensemble of simulations. For a system in equilibrium we have

$$\begin{aligned} \frac{dP(x,t)}{dt} = 0 &\implies E[x(t_1)] = E[x(t_0)] = \langle x \rangle \\ &\implies E[x(t_1)x(t_0)] = \langle x(0)x(t_1 - t_0) \rangle \end{aligned}$$

Where  $\langle \cdot \rangle$  is an average over time point measurements.

The autocorrelation function is defined as

$$A(t) = \frac{\langle x(0)x(t) \rangle - \langle x \rangle^2}{\langle x^2 \rangle - \langle x \rangle^2}$$

So that  $A(0) = 1$  and  $A(\infty) = 0$ .

The autocorrelation function becomes a stretched exponential in the region of bistability.